

$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

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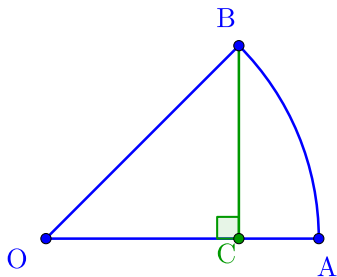
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▶ End

$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

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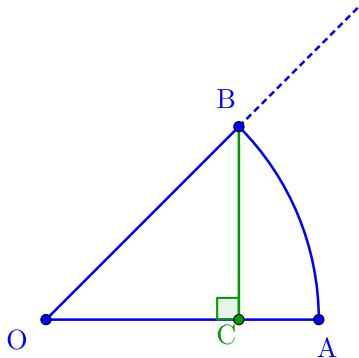
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$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

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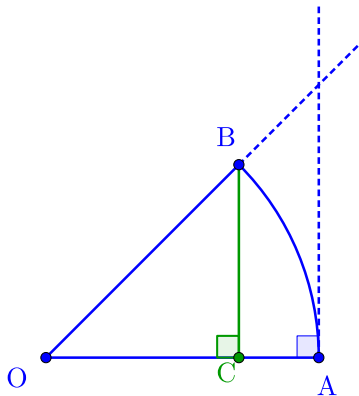
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$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

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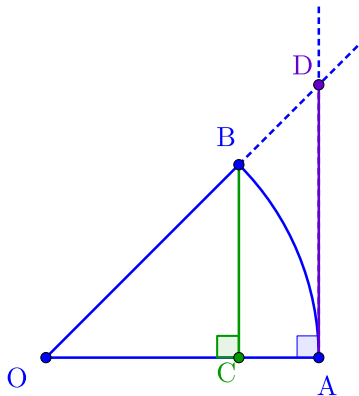
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$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

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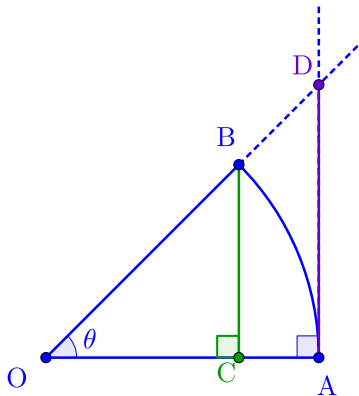
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$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

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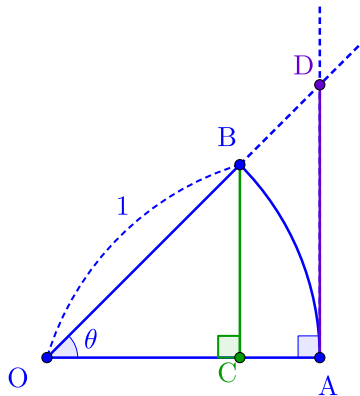
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$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

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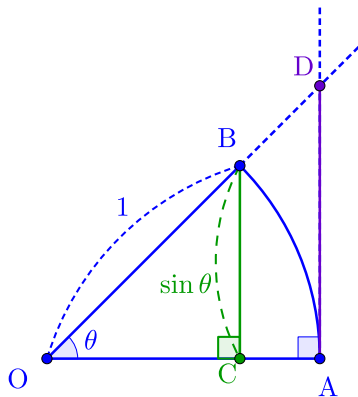
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▶ Start

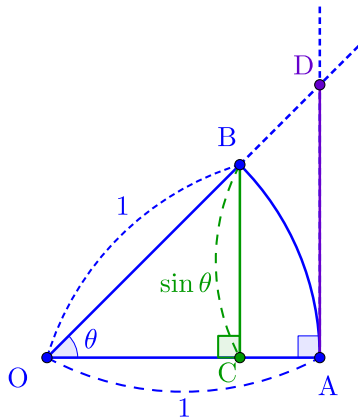
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▶ Start

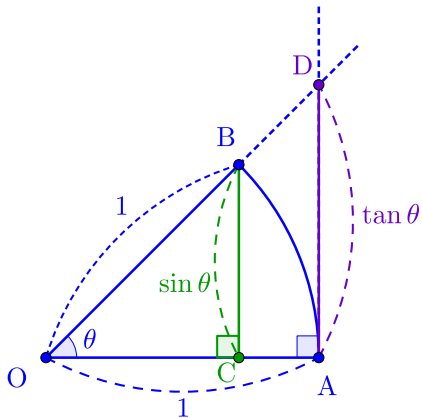
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$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

▶ Start

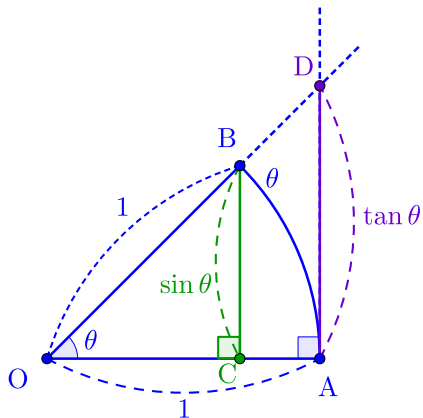
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$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

▶ Start

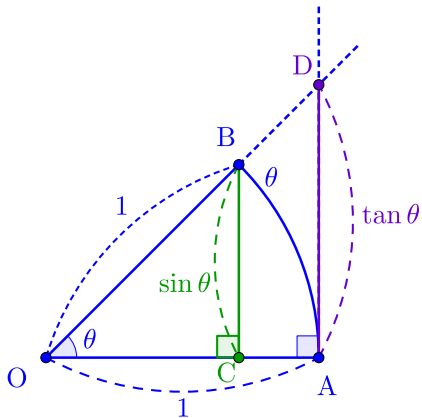
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$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

▶ Start

▶ End

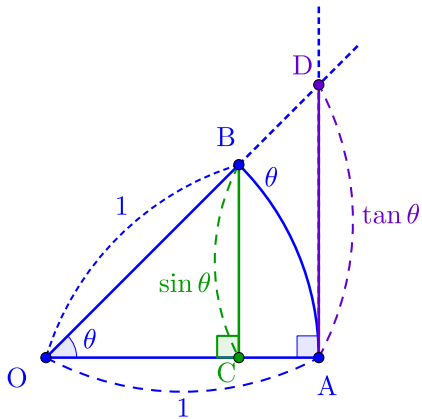


$$\overline{BC} < \text{arc } AB$$

$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

▶ Start

▶ End



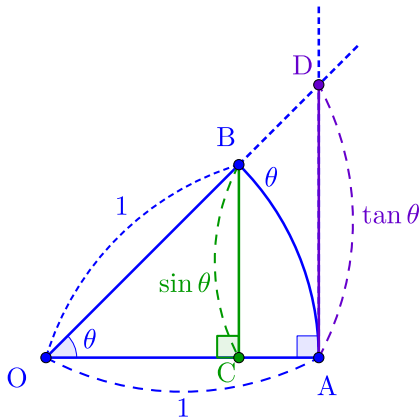
$$\overline{BC} < \text{arc } AB$$

$$\sin \theta < \theta$$

$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

▶ Start

▶ End



$$\overline{BC} < \text{arc AB}$$

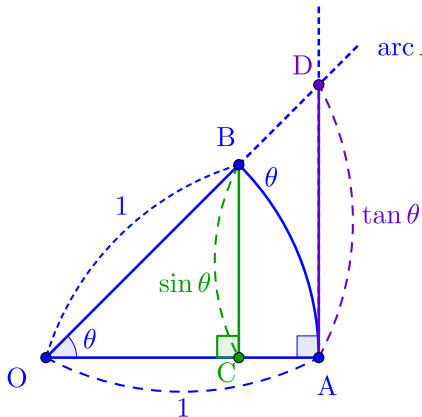
$$\sin \theta < \theta$$

$$\frac{\sin \theta}{\theta} < 1$$

$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

▶ Start

▶ End



$$\text{arc } AB < \overline{AD}$$

$$\overline{BC} < \text{arc } AB$$

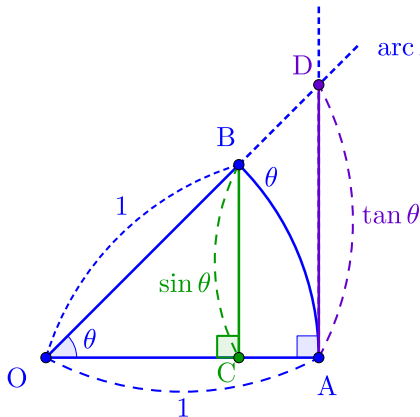
$$\sin \theta < \theta$$

$$\frac{\sin \theta}{\theta} < 1$$

$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

▶ Start

▶ End



$$\text{arc } AB < \overline{AD} \quad \overline{BC} < \text{arc } AB$$

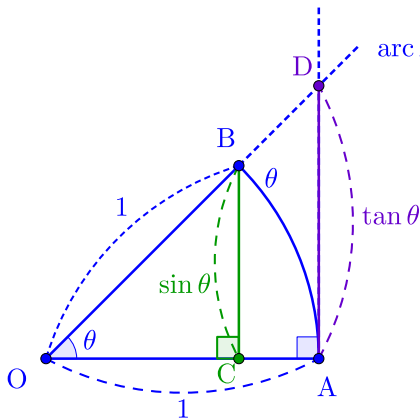
$$\theta < \tan \theta \quad \sin \theta < \theta$$

$$\frac{\sin \theta}{\theta} < 1$$

$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

▶ Start

▶ End



$$\text{arc AB} < \overline{AD} \quad \overline{BC} < \text{arc AB}$$

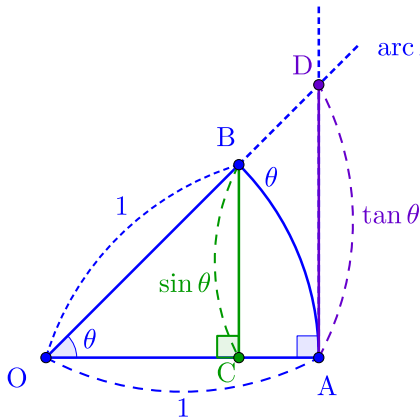
$$\theta < \tan \theta \quad \sin \theta < \theta$$

$$\cos \theta < \frac{\sin \theta}{\theta} < 1$$

$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

▶ Start

▶ End



$$\text{arc } AB < \overline{AD} \quad \overline{BC} < \text{arc } AB$$

$$\theta < \tan \theta \quad \sin \theta < \theta$$

$$\cos \theta < \frac{\sin \theta}{\theta} < 1$$

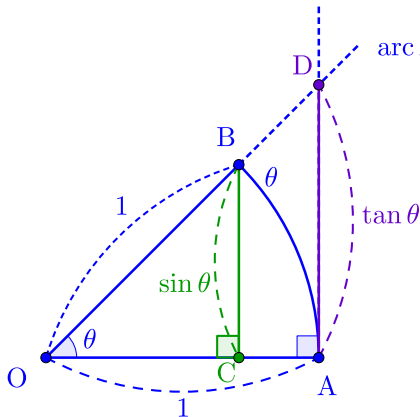
$$\lim_{\theta \rightarrow 0^+} \cos \theta = 1$$

$$\lim_{\theta \rightarrow 0^+} \frac{\sin \theta}{\theta} = 1$$

$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

▶ Start

▶ End



$$\text{arc AB} < \overline{AD} \quad \overline{BC} < \text{arc AB}$$

$$\theta < \tan \theta \quad \sin \theta < \theta$$

$$\cos \theta < \frac{\sin \theta}{\theta} < 1$$

$$\lim_{\theta \rightarrow 0^+} \cos \theta = 1$$

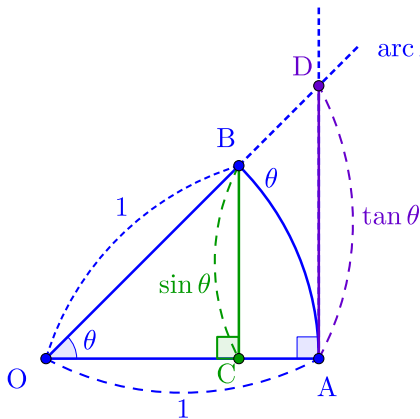
$$\lim_{\theta \rightarrow 0^+} \frac{\sin \theta}{\theta} = 1$$

$$(\because \frac{\sin \theta}{\theta} \text{ is even.})$$

$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

▶ Start

▶ End



$$\text{arc } AB < \overline{AD} \quad \overline{BC} < \text{arc } AB$$

$$\theta < \tan \theta \quad \sin \theta < \theta$$

$$\cos \theta < \frac{\sin \theta}{\theta} < 1$$

$$\lim_{\theta \rightarrow 0^+} \cos \theta = 1$$

$$\lim_{\theta \rightarrow 0^+} \frac{\sin \theta}{\theta} = 1$$

($\because \frac{\sin \theta}{\theta}$ is even.)

$$\therefore \lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

Github:

<https://min7014.github.io/math20240217001.html>

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and you can see a picture moving.