## The derivative of f

함수f의 미분 (The derivative of f)

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# Definition

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f'(x)





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$$\frac{dy}{dx}$$

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D,  $\frac{d}{dx}$ : the differentiation operators

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A function f is differentiable at a if f'(a) exists. It is differentiable on an open interval (a,b) [or  $(a,\infty)$  or  $(-\infty,a)$  or  $(-\infty,\infty)$  ] if it is differentiable at every number in the interval.

#### Github:

https://min7014.github.io/math20240130001.html

Click or paste URL into the URL search bar, and you can see a picture moving.