

Formulas that transform sums or differences of trigonometric functions into products

삼각함수의 합 또는 차를 곱으로 변형하는 공식
(Formulas that transform sums or differences of trigonometric functions into products)

Formulas that transform sums or differences of trigonometric functions into products

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Formulas that transform sums or differences of trigonometric functions into products

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$$\sin A + \sin B =$$

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$$\sin A + \sin B = 2 \sin \frac{A+B}{2} \cos \frac{A-B}{2} \quad \text{▶ proof}$$

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$$\sin A + \sin B = 2 \sin \frac{A+B}{2} \cos \frac{A-B}{2} \quad \text{▶ proof}$$

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$$\sin A + \sin B = 2 \sin \frac{A+B}{2} \cos \frac{A-B}{2} \quad \text{▶ proof}$$

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$$\sin \alpha \cos \beta = \frac{1}{2} \{ \sin(\alpha + \beta) + \sin(\alpha - \beta) \}$$

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$$\begin{aligned}\sin \alpha \cos \beta &= \frac{1}{2} \{ \sin(\alpha + \beta) + \sin(\alpha - \beta) \} \\ 2 \sin \alpha \cos \beta &= \sin(\alpha + \beta) + \sin(\alpha - \beta)\end{aligned}$$

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$$\begin{aligned}\sin \alpha \cos \beta &= \frac{1}{2} \{ \sin(\alpha + \beta) + \sin(\alpha - \beta) \} \\ 2 \sin \alpha \cos \beta &= \sin(\alpha + \beta) + \sin(\alpha - \beta) \\ \sin(\alpha + \beta) + \sin(\alpha - \beta) &= 2 \sin \alpha \cos \beta\end{aligned}$$

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$$\textit{Let } A = \alpha + \beta, B = \alpha - \beta$$

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$$\therefore \sin A + \sin B = 2 \sin \frac{A + B}{2} \cos \frac{A - B}{2}$$

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$$\cos \alpha \sin \beta = \frac{1}{2} \{ \sin(\alpha + \beta) - \sin(\alpha - \beta) \}$$

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$$\begin{aligned}\cos \alpha \sin \beta &= \frac{1}{2} \{ \sin(\alpha + \beta) - \sin(\alpha - \beta) \} \\ 2 \cos \alpha \sin \beta &= \sin(\alpha + \beta) - \sin(\alpha - \beta)\end{aligned}$$

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$$\begin{aligned}\cos \alpha \sin \beta &= \frac{1}{2} \{ \sin(\alpha + \beta) - \sin(\alpha - \beta) \} \\ 2 \cos \alpha \sin \beta &= \sin(\alpha + \beta) - \sin(\alpha - \beta) \\ \sin(\alpha + \beta) - \sin(\alpha - \beta) &= 2 \cos \alpha \sin \beta\end{aligned}$$

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$$\begin{aligned}\sin \alpha \sin \beta &= -\frac{1}{2} \{ \cos(\alpha + \beta) - \cos(\alpha - \beta) \} \\ -2 \sin \alpha \sin \beta &= \cos(\alpha + \beta) - \cos(\alpha - \beta)\end{aligned}$$

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Github:

<https://min7014.github.io/math20230423001.html>

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