

## 삼각함수의 반각 공식

(Half Angle Formula for Trigonometric Functions)

# Half Angle Formula for Trigonometric Functions

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# Half Angle Formula for Trigonometric Functions

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$$\sin^2 \frac{\alpha}{2} =$$

# Half Angle Formula for Trigonometric Functions

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$$\sin^2 \frac{\alpha}{2} = \frac{1 - \cos \alpha}{2}$$

# Half Angle Formula for Trigonometric Functions

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$$\sin^2 \frac{\alpha}{2} = \frac{1 - \cos \alpha}{2}$$

▶ proof

$$\cos^2 \frac{\alpha}{2} =$$

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$$\sin^2 \frac{\alpha}{2} = \frac{1 - \cos \alpha}{2}$$

▶ proof

$$\cos^2 \frac{\alpha}{2} = \frac{1 + \cos \alpha}{2}$$

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$$\sin^2 \frac{\alpha}{2} = \frac{1 - \cos \alpha}{2}$$

▶ proof

$$\cos^2 \frac{\alpha}{2} = \frac{1 + \cos \alpha}{2}$$

▶ proof

$$\tan^2 \frac{\alpha}{2} =$$

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$$\sin^2 \frac{\alpha}{2} = \frac{1 - \cos \alpha}{2}$$

▶ proof

$$\cos^2 \frac{\alpha}{2} = \frac{1 + \cos \alpha}{2}$$

▶ proof

$$\tan^2 \frac{\alpha}{2} = \frac{1 - \cos \alpha}{1 + \cos \alpha}$$

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$$\sin^2 \frac{\alpha}{2} = \frac{1 - \cos \alpha}{2}$$

▶ proof

$$\cos^2 \frac{\alpha}{2} = \frac{1 + \cos \alpha}{2}$$

▶ proof

$$\tan^2 \frac{\alpha}{2} = \frac{1 - \cos \alpha}{1 + \cos \alpha}$$

▶ proof

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# Half Angle Formula for Trigonometric Functions

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$$\cos \alpha =$$

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$$\cos \alpha = \cos \left( 2 \cdot \frac{\alpha}{2} \right)$$

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$$\begin{aligned}\cos \alpha &= \cos \left( 2 \cdot \frac{\alpha}{2} \right) \\ &= 1 - 2 \sin^2 \frac{\alpha}{2}\end{aligned}$$

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$$\cos \alpha = \cos \left( 2 \cdot \frac{\alpha}{2} \right)$$

$$= 1 - 2 \sin^2 \frac{\alpha}{2}$$

$$2 \sin^2 \frac{\alpha}{2} =$$

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$$\cos \alpha = \cos \left( 2 \cdot \frac{\alpha}{2} \right)$$

$$= 1 - 2 \sin^2 \frac{\alpha}{2}$$

$$2 \sin^2 \frac{\alpha}{2} = 1 - \cos \alpha$$

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$$\cos \alpha = \cos \left( 2 \cdot \frac{\alpha}{2} \right)$$

$$= 1 - 2 \sin^2 \frac{\alpha}{2}$$

$$2 \sin^2 \frac{\alpha}{2} = 1 - \cos \alpha$$

$$\therefore \sin^2 \frac{\alpha}{2} =$$

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$$\cos \alpha = \cos \left( 2 \cdot \frac{\alpha}{2} \right)$$

$$= 1 - 2 \sin^2 \frac{\alpha}{2}$$

$$2 \sin^2 \frac{\alpha}{2} = 1 - \cos \alpha$$

$$\therefore \sin^2 \frac{\alpha}{2} = \frac{1 - \cos \alpha}{2}$$

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$$\cos \alpha =$$

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$$\cos \alpha = \cos \left( 2 \cdot \frac{\alpha}{2} \right)$$

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$$\begin{aligned}\cos \alpha &= \cos\left(2 \cdot \frac{\alpha}{2}\right) \\ &= 2 \cos^2 \frac{\alpha}{2} - 1\end{aligned}$$

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$$\begin{aligned}\cos \alpha &= \cos\left(2 \cdot \frac{\alpha}{2}\right) \\ &= 2 \cos^2 \frac{\alpha}{2} - 1\end{aligned}$$

$$\cos \alpha + 1 =$$

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$$\cos \alpha = \cos \left( 2 \cdot \frac{\alpha}{2} \right)$$

$$= 2 \cos^2 \frac{\alpha}{2} - 1$$

$$\cos \alpha + 1 = 2 \cos^2 \frac{\alpha}{2}$$

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$$\cos \alpha = \cos \left( 2 \cdot \frac{\alpha}{2} \right)$$

$$= 2 \cos^2 \frac{\alpha}{2} - 1$$

$$\cos \alpha + 1 = 2 \cos^2 \frac{\alpha}{2}$$

$$\therefore \cos^2 \frac{\alpha}{2} =$$

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$$\cos \alpha = \cos \left( 2 \cdot \frac{\alpha}{2} \right)$$

$$= 2 \cos^2 \frac{\alpha}{2} - 1$$

$$\cos \alpha + 1 = 2 \cos^2 \frac{\alpha}{2}$$

$$\therefore \cos^2 \frac{\alpha}{2} = \frac{1 + \cos \alpha}{2}$$

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$$\tan^2 \frac{\alpha}{2} =$$

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$$\tan^2 \frac{\alpha}{2} = \frac{\sin^2 \frac{\alpha}{2}}{\cos^2 \frac{\alpha}{2}}$$

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$$\tan^2 \frac{\alpha}{2} = \frac{\sin^2 \frac{\alpha}{2}}{\cos^2 \frac{\alpha}{2}}$$

$$= \frac{\frac{1 - \cos \alpha}{2}}{\frac{1 + \cos \alpha}{2}}$$

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$$\tan^2 \frac{\alpha}{2} = \frac{\sin^2 \frac{\alpha}{2}}{\cos^2 \frac{\alpha}{2}}$$

$$= \frac{\frac{1 - \cos \alpha}{2}}{\frac{1 + \cos \alpha}{2}}$$

$$\therefore \tan^2 \frac{\alpha}{2} = \frac{1 - \cos \alpha}{1 + \cos \alpha}$$

Github:

<https://min7014.github.io/math20230421001.html>

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and you can see a picture moving.