

삼각함수의 합성(일반각)

(Composition of Trigonometric Functions (Ggeneral Angle))

Composition of Trigonometric Functions (Ggeneral Angle)

▶ Start

▶ End

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▶ Start

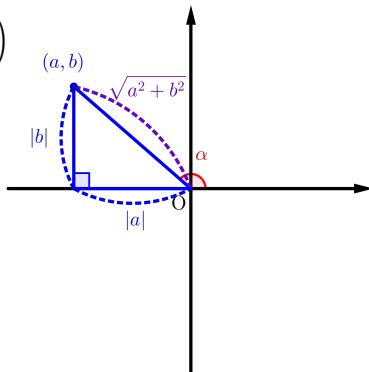
▶ End

Composition of Trigonometric Functions (General Angle)

▶ Start

▶ End

$$\begin{aligned} & a \sin \theta + b \cos \theta \quad (ab \neq 0) \\ &= \sqrt{a^2 + b^2} \left(\frac{a}{\sqrt{a^2 + b^2}} \sin \theta + \frac{b}{\sqrt{a^2 + b^2}} \cos \theta \right) \\ &= \sqrt{a^2 + b^2} (\cos \alpha \end{aligned}$$

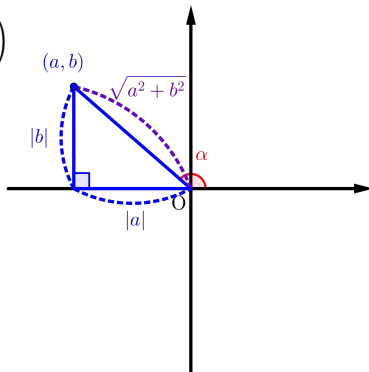


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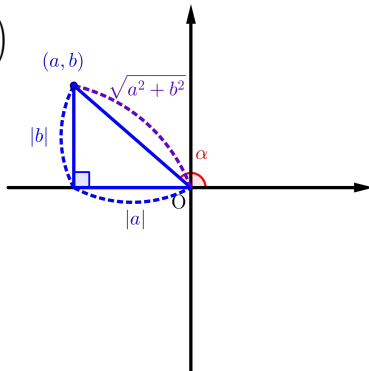


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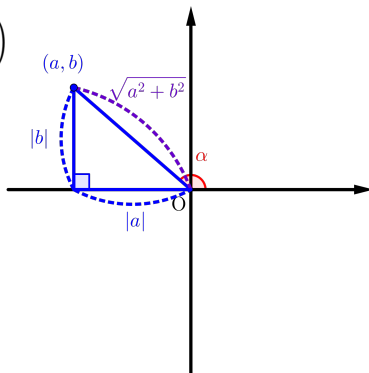


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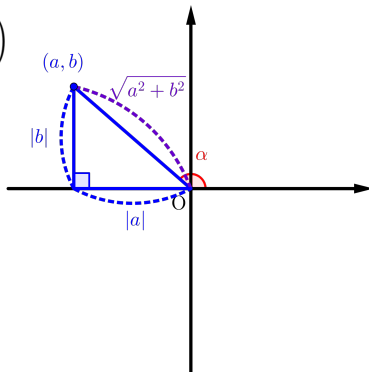


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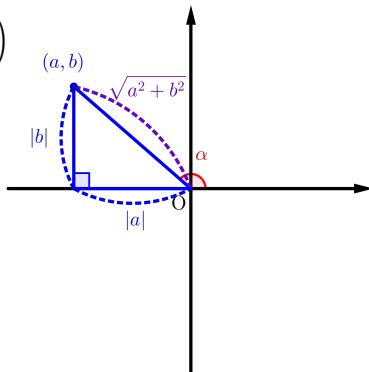


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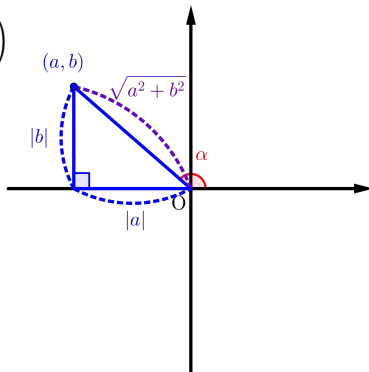


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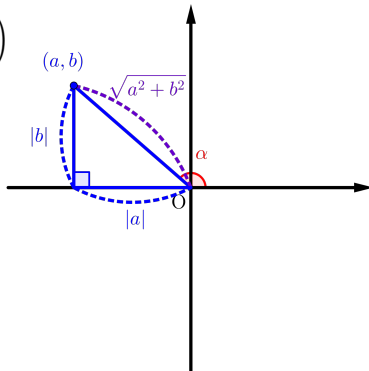


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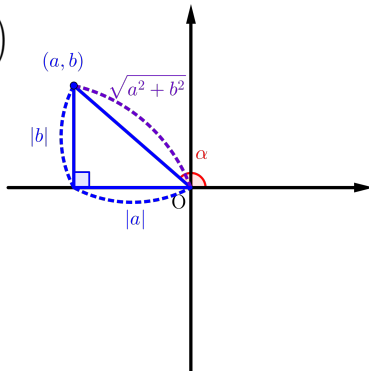


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Composition of Trigonometric Functions (General Angle)

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$$a \sin \theta + b \cos \theta \quad (ab \neq 0)$$

$$= \sqrt{a^2 + b^2} \left(\frac{a}{\sqrt{a^2 + b^2}} \sin \theta + \frac{b}{\sqrt{a^2 + b^2}} \cos \theta \right)$$

$$= \sqrt{a^2 + b^2} (\cos \alpha \sin \theta + \sin \alpha \cos \theta)$$

$$= \sqrt{a^2 + b^2} (\sin \theta \cos \alpha + \cos \theta \sin \alpha)$$

$$= \sqrt{a^2 + b^2} \sin(\theta + \alpha)$$

$$\therefore a \sin \theta + b \cos \theta = \sqrt{a^2 + b^2} \sin(\theta + \alpha)$$

$$\left(\cos \alpha = \frac{a}{\sqrt{a^2 + b^2}}, \quad \sin \alpha = \frac{b}{\sqrt{a^2 + b^2}} \right)$$

$$a \sin \theta + b \cos \theta \quad (ab \neq 0)$$

(a, b)



Composition of Trigonometric Functions (General Angle)

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$$a \sin \theta + b \cos \theta \quad (ab \neq 0)$$

$$= \sqrt{a^2 + b^2} \left(\frac{a}{\sqrt{a^2 + b^2}} \sin \theta + \frac{b}{\sqrt{a^2 + b^2}} \cos \theta \right)$$

$$= \sqrt{a^2 + b^2} (\cos \alpha \sin \theta + \sin \alpha \cos \theta)$$

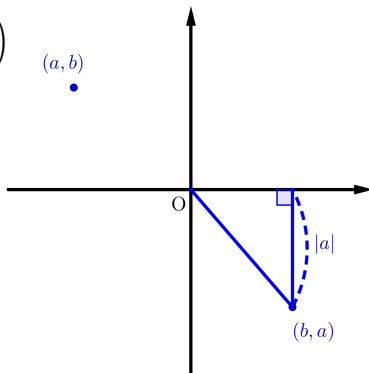
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$$= \sqrt{a^2 + b^2} \sin(\theta + \alpha)$$

$$\therefore a \sin \theta + b \cos \theta = \sqrt{a^2 + b^2} \sin(\theta + \alpha)$$

$$\left(\cos \alpha = \frac{a}{\sqrt{a^2 + b^2}}, \quad \sin \alpha = \frac{b}{\sqrt{a^2 + b^2}} \right)$$

$$a \sin \theta + b \cos \theta \quad (ab \neq 0)$$



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$$= \sqrt{a^2 + b^2} \left(\frac{a}{\sqrt{a^2 + b^2}} \sin \theta + \frac{b}{\sqrt{a^2 + b^2}} \cos \theta \right)$$

$$= \sqrt{a^2 + b^2} (\cos \alpha \sin \theta + \sin \alpha \cos \theta)$$

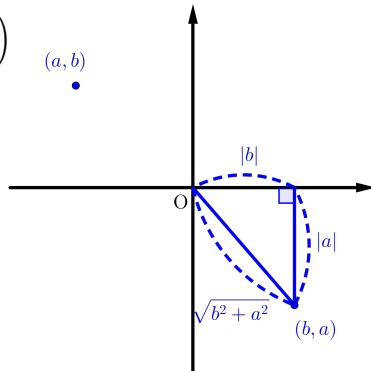
$$= \sqrt{a^2 + b^2} (\sin \theta \cos \alpha + \cos \theta \sin \alpha)$$

$$= \sqrt{a^2 + b^2} \sin(\theta + \alpha)$$

$$\therefore a \sin \theta + b \cos \theta = \sqrt{a^2 + b^2} \sin(\theta + \alpha)$$

$$\left(\cos \alpha = \frac{a}{\sqrt{a^2 + b^2}}, \quad \sin \alpha = \frac{b}{\sqrt{a^2 + b^2}} \right)$$

$$a \sin \theta + b \cos \theta \quad (ab \neq 0)$$



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$$= \sqrt{a^2 + b^2} \left(\frac{a}{\sqrt{a^2 + b^2}} \sin \theta + \frac{b}{\sqrt{a^2 + b^2}} \cos \theta \right)$$

$$= \sqrt{a^2 + b^2} (\cos \alpha \sin \theta + \sin \alpha \cos \theta)$$

$$= \sqrt{a^2 + b^2} (\sin \theta \cos \alpha + \cos \theta \sin \alpha)$$

$$= \sqrt{a^2 + b^2} \sin(\theta + \alpha)$$

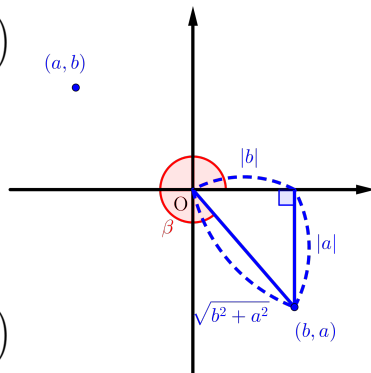
$$\therefore a \sin \theta + b \cos \theta = \sqrt{a^2 + b^2} \sin(\theta + \alpha)$$

$$\left(\cos \alpha = \frac{a}{\sqrt{a^2 + b^2}}, \quad \sin \alpha = \frac{b}{\sqrt{a^2 + b^2}} \right)$$

$$a \sin \theta + b \cos \theta \quad (ab \neq 0)$$

$$= \sqrt{a^2 + b^2} \left(\frac{a}{\sqrt{a^2 + b^2}} \sin \theta + \frac{b}{\sqrt{a^2 + b^2}} \cos \theta \right)$$

$$= \sqrt{a^2 + b^2} ($$



Github:

<https://min7014.github.io/math20230418001.html>

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and you can see a picture moving.