

(When a directrix is  $x = -p$  and a focus is  $(p, 0)$ , find the equation for the tangent line to the parabola at a given point  $(x_1, y_1)$ .)

준선이  $x = -p$  이고 초점이  $(p, 0)$  일 때, 포물선 상의 점  $(x_1, y_1)$  에서의 접선의 방정식을 구하여라.[기하적 접근]

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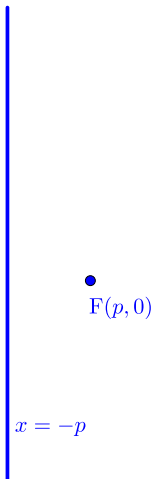


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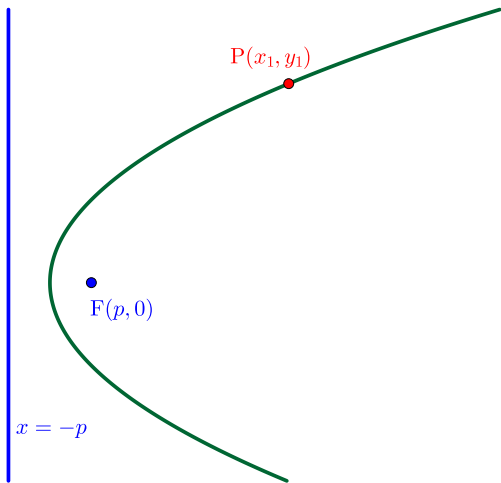




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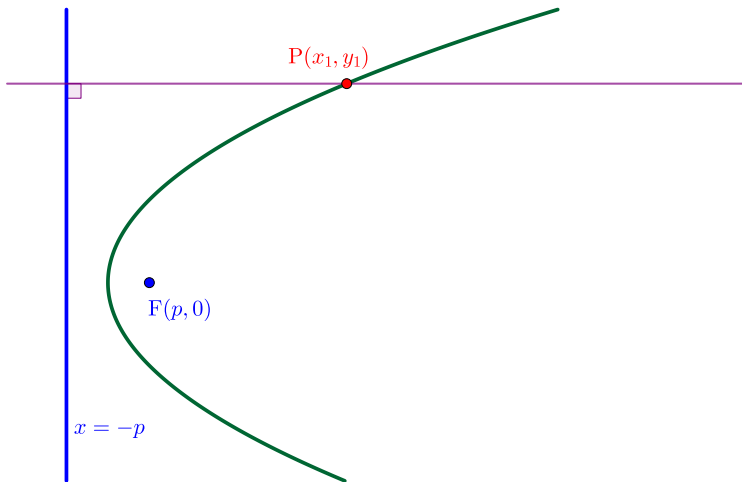
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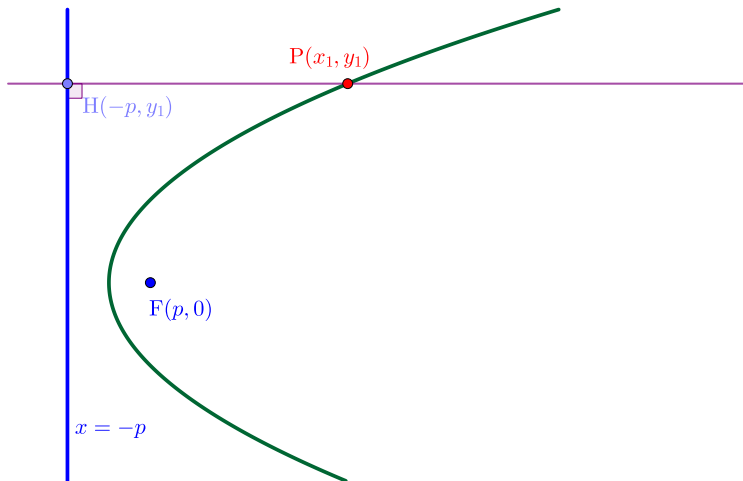
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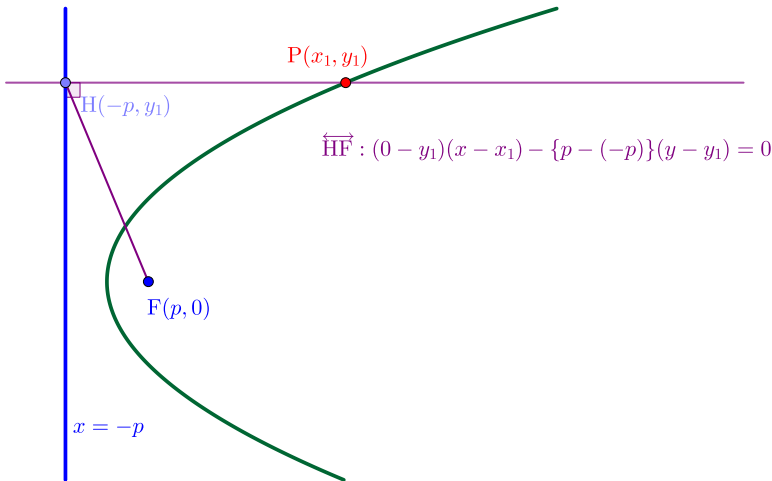




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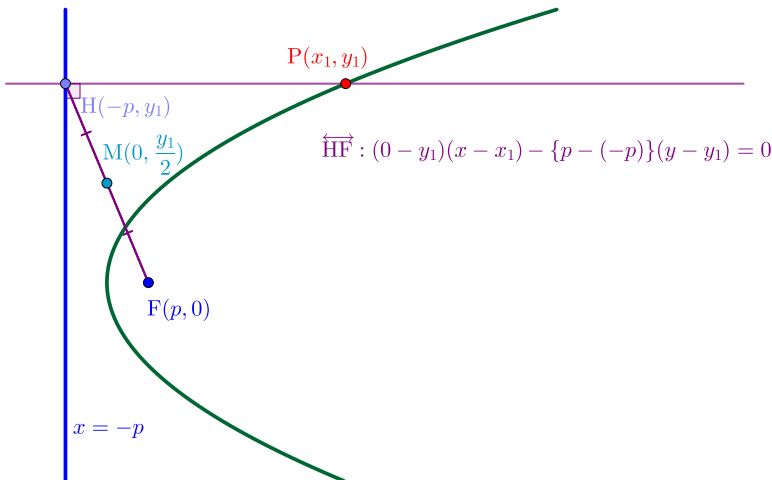
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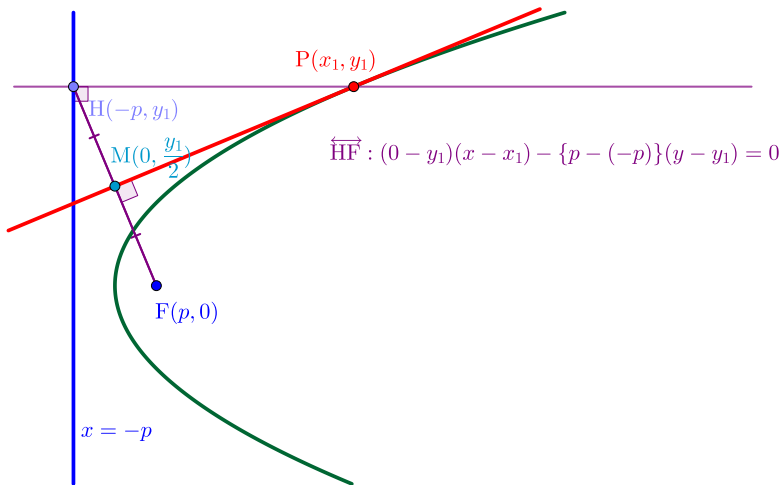
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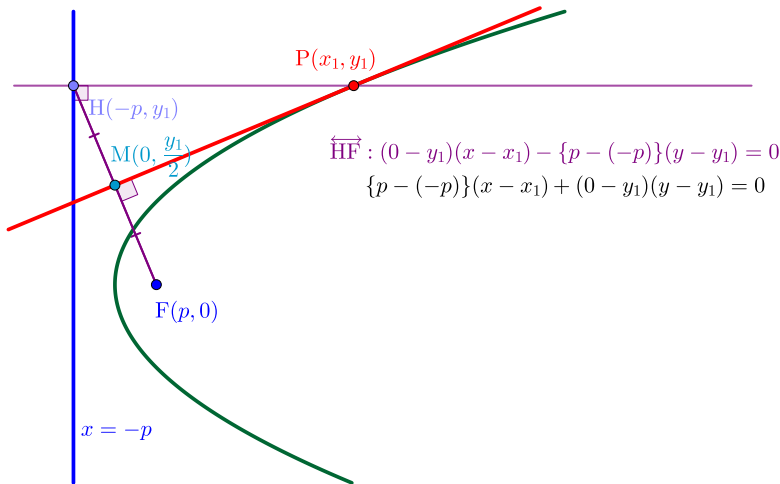
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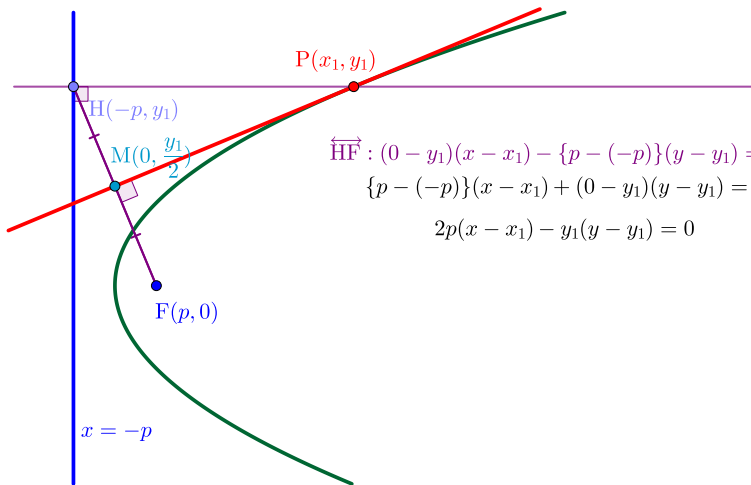
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$$\overrightarrow{HP}: (0 - y_1)(x - x_1) - \{p - (-p)\}(y - y_1) = 0$$

$$\{p - (-p)\}(x - x_1) + (0 - y_1)(y - y_1) = 0$$

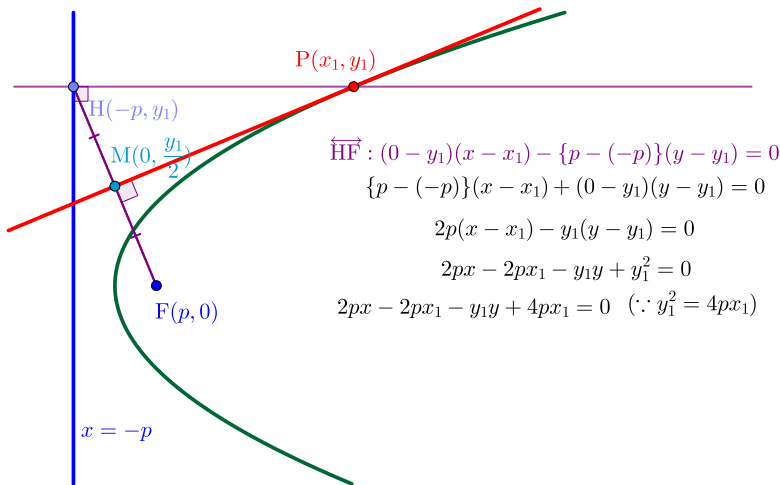
$$2p(x - x_1) - y_1(y - y_1) = 0$$



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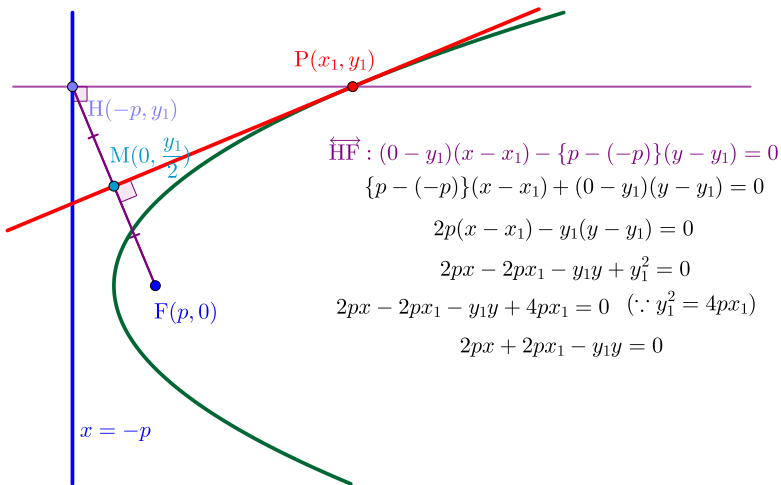
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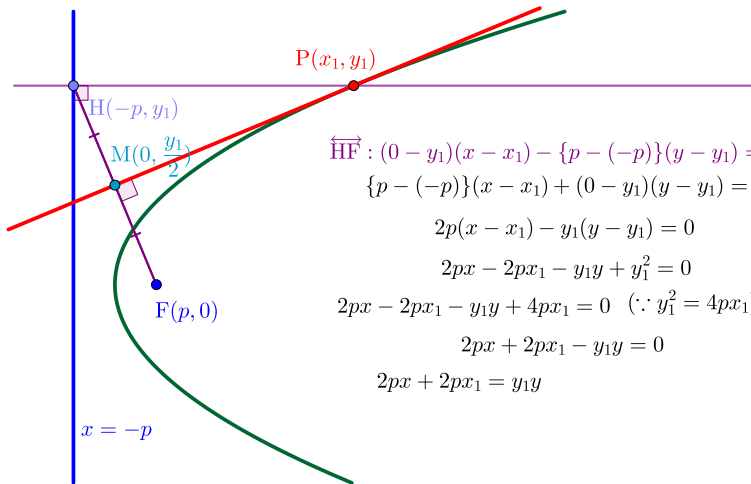
$$\begin{aligned} \overrightarrow{HF} &: (0 - y_1)(x - x_1) - \{p - (-p)\}(y - y_1) = 0 \\ \{p - (-p)\}(x - x_1) + (0 - y_1)(y - y_1) &= 0 \\ 2p(x - x_1) - y_1(y - y_1) &= 0 \\ 2px - 2px_1 - y_1y + y_1^2 &= 0 \\ 2px - 2px_1 - y_1y + 4px_1 &= 0 \quad (\because y_1^2 = 4px_1) \\ 2px + 2px_1 - y_1y &= 0 \end{aligned}$$



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$$2px - 2px_1 - y_1y + 4px_1 = 0 \quad (\because y_1^2 = 4px_1)$$

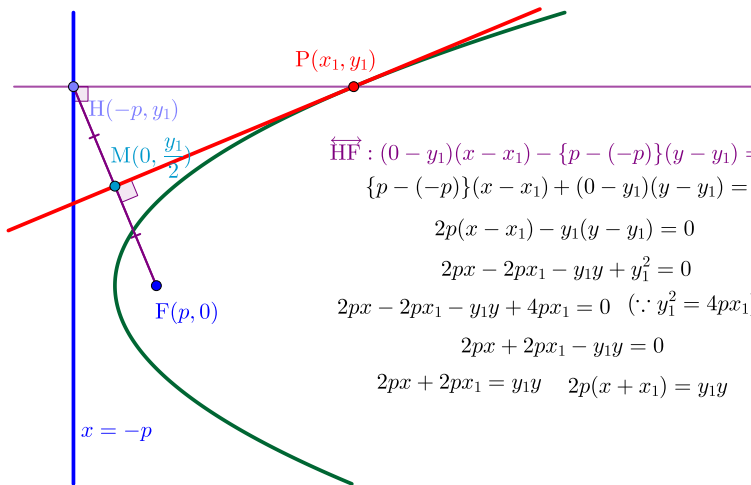
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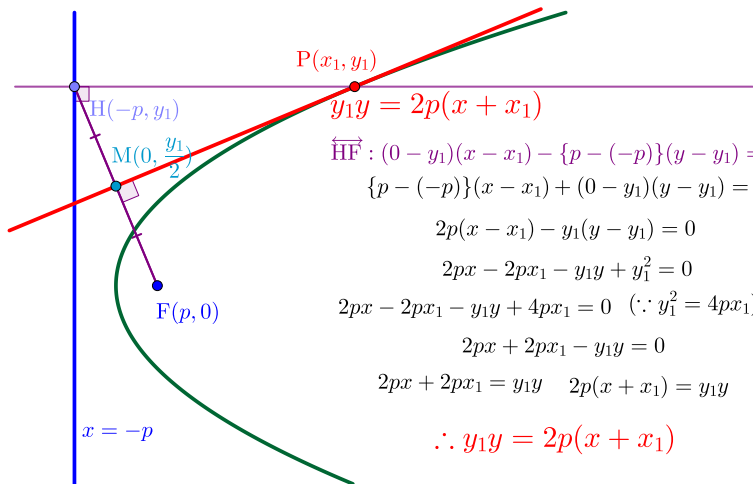
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$$2px + 2px_1 = y_1y \quad 2p(x + x_1) = y_1y$$

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$$y_1 y = 2p(x + x_1)$$

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$$2p(x - x_1) - y_1(y - y_1) = 0$$

$$2px - 2px_1 - y_1 y + y_1^2 = 0$$

$$2px - 2px_1 - y_1 y + 4px_1 = 0 \quad (\because y_1^2 = 4px_1)$$

$$2px + 2px_1 - y_1 y = 0$$

$$2px + 2px_1 = y_1 y \quad 2p(x + x_1) = y_1 y$$

$$\therefore y_1 y = 2p(x + x_1)$$

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Github:

<https://min7014.github.io/math20220301001.html>

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and you can see a picture moving.