분수방정식의 결합형 예제
(Combined Example of Fractional Equations)

Combined Example of Fractional Equations

Start End

$$\frac{1}{x-1}+\frac{1}{x-3}+\frac{1}{x-7}+\frac{1}{x-9} = 0 \cdots (1)$$

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(1)식의 분모를 0으로 만들지 않으므로

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(1)식의 분모를 0으로 만들지 않으므로

$$\therefore\ x = 5, 5\pm\sqrt{10}$$

Github:
https://min7014.github.io/math20210211001.html

Click or paste URL into the URL search bar, and you can see a picture moving.