켤레복소수의 해에 관한 정리
(The Complex Conjugate Root Theorem)

▸ Start ▸ End

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The Complex Conjugate Root Theorem

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The Complex Conjugate Root Theorem

$f(x) = a_n x^n + a_{n-1} x^{n-1} + \cdots + a_0$

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Start End

The Complex Conjugate Root Theorem

$$f(x) = a_n x^n + a_{n-1} x^{n-1} + \cdots + a_0 \; (a_i \in \mathbb{R},\; a_n \neq 0)$$

$$f(z) = 0 \Rightarrow f(\overline{z}) = 0$$

Start End

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If $f(x)$ is a polynomial

▸ Start ▸ End

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Start End

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If $f(x)$ is a polynomial with real coefficients, and z is a root

Start End

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Start End

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$$\overline{f(z)}$$

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$$\therefore\ f(\overline{z}) = 0$$

Github:
https://min7014.github.io/math20210127001.html

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