Polynomial Remainder Theorem

- $f(x)$: *a polynomial*

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Github:
https://min7014.github.io/math20201220002.html

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