

Euclid's Lemma

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$$a|bc$$

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▶ proof

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▶ proof

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$\exists x,$

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$\exists x, y$

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$\exists x, y \in$

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$$\exists x, y \in \mathbb{Z}$$

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$\exists x, y \in \mathbb{Z}$ such that $1 =$

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$\exists x, y \in \mathbb{Z}$ such that $1 = ax$

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$\exists x, y \in \mathbb{Z}$ such that $1 = ax +$

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$\exists x, y \in \mathbb{Z}$ such that $1 = ax + by$ (\because

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$$c = 1 \times c = (ax + by)c = acx + bcy$$

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$a \mid$

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$$\therefore a|c$$

Github:

<https://min7014.github.io/math20201211001.html>

Click or paste URL into the URL search bar,
and you can see a picture moving.