두 초점이 $(0, k)$, $(0, -k)$ 이고 길이의 차가 $2b$ 로 주어 졌을 때 쌍곡선의 방정식

(The equation for hyperbola when the two focal points are $(0, k)$, $(0, -k)$ and the difference in length is given by $2b$)

The equation for hyperbola when the two focal points are $(0, k)$, $(0, -k)$ and the difference in length is given by $2b$

▸ Start ▸ End

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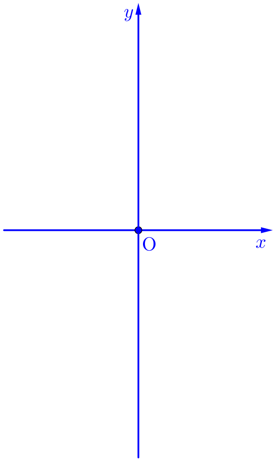
Start End



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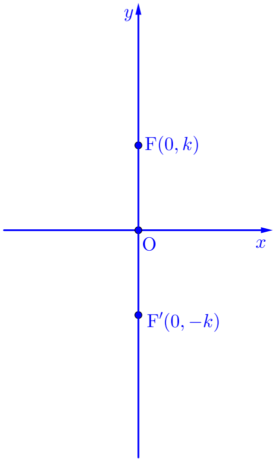

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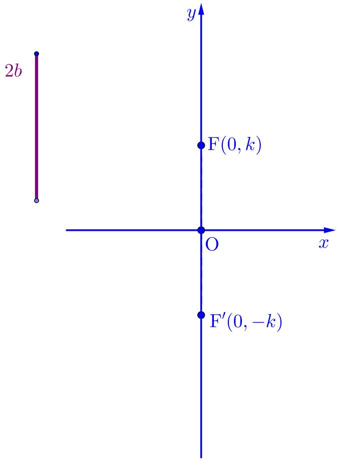

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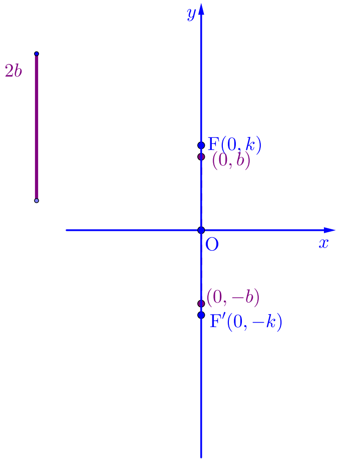

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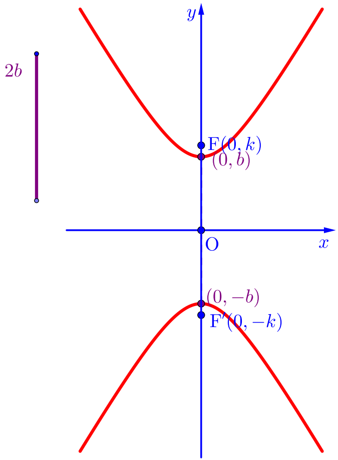

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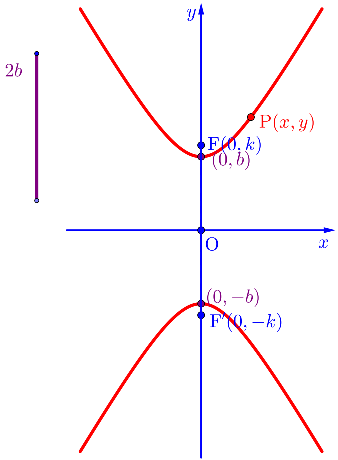

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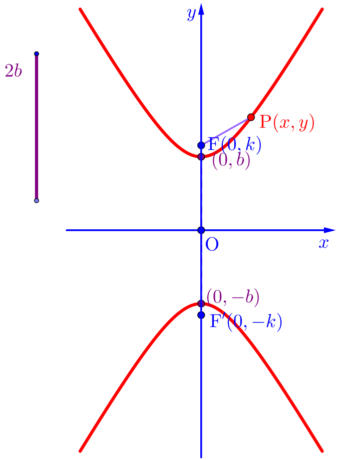

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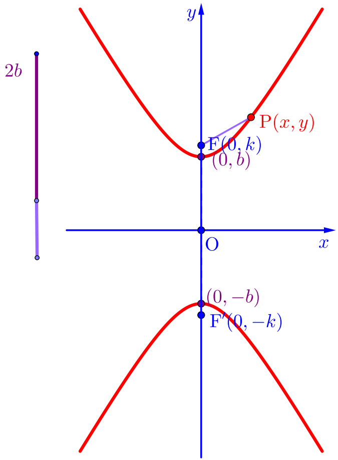

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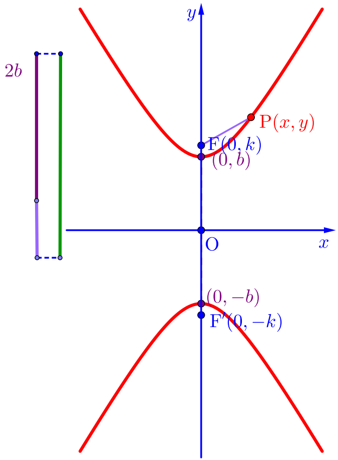

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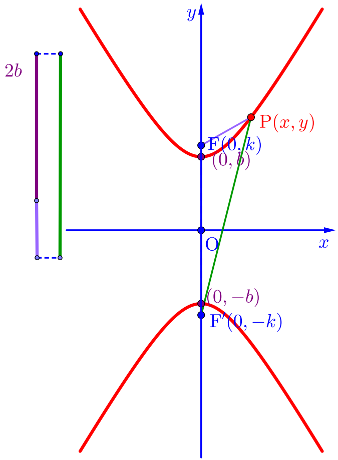

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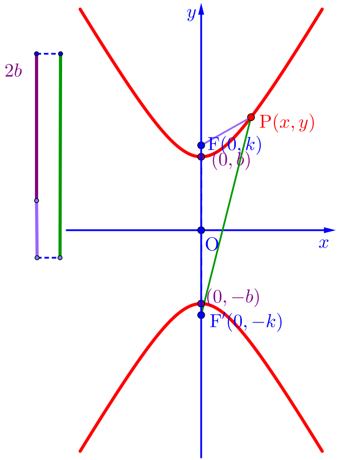

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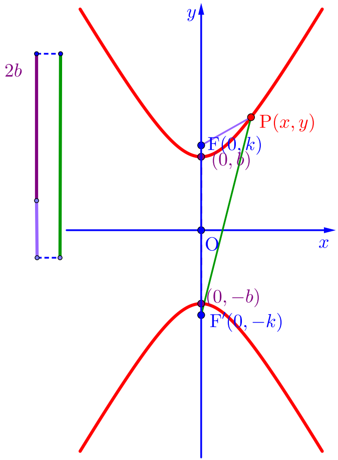

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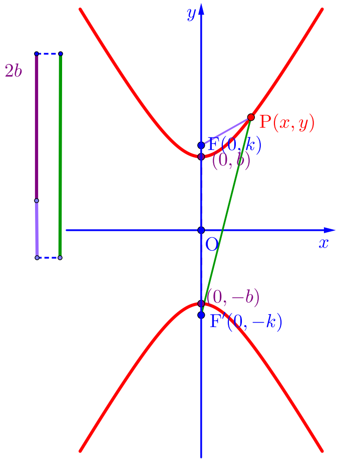

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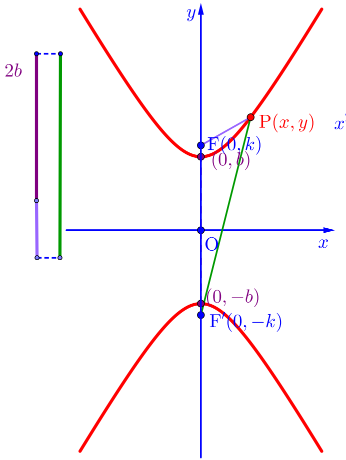

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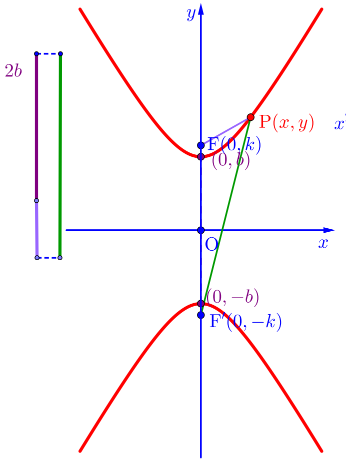

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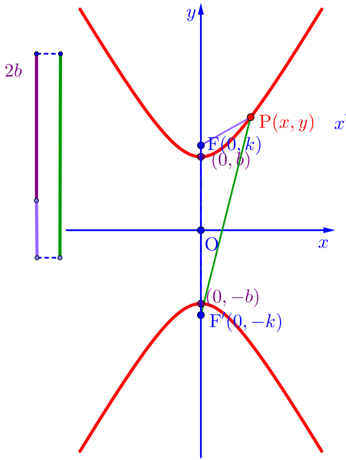

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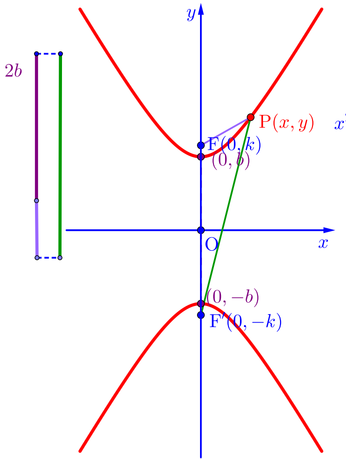

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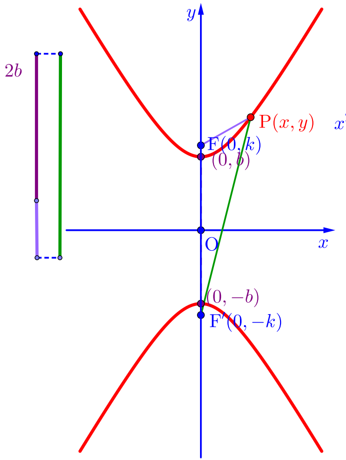

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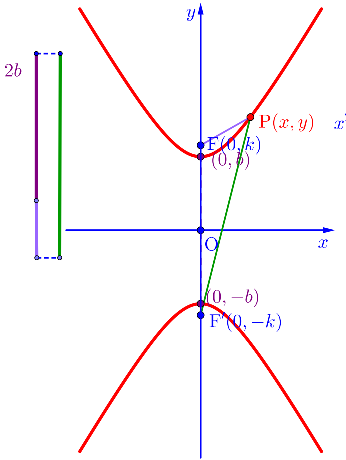

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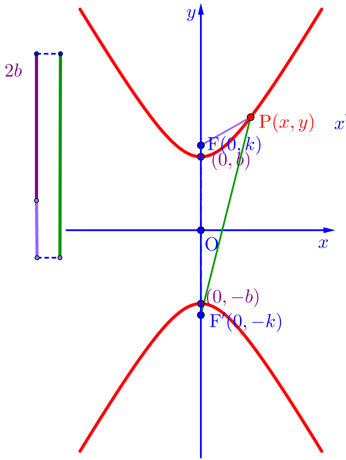

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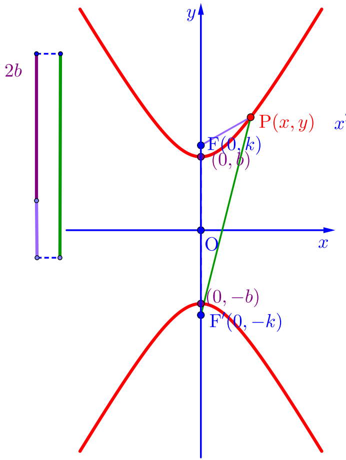

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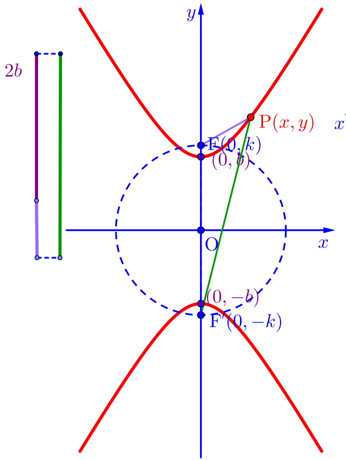

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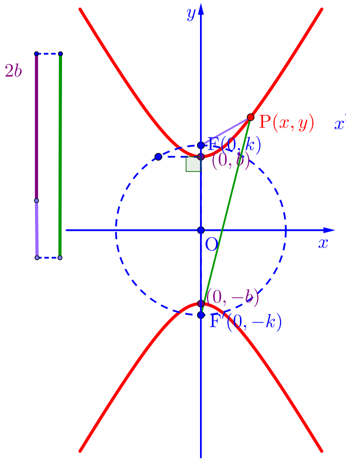

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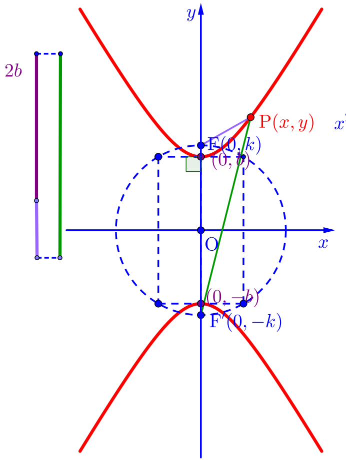

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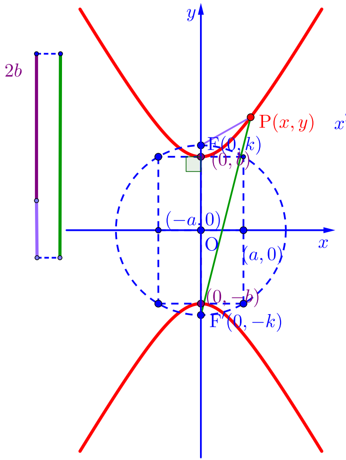

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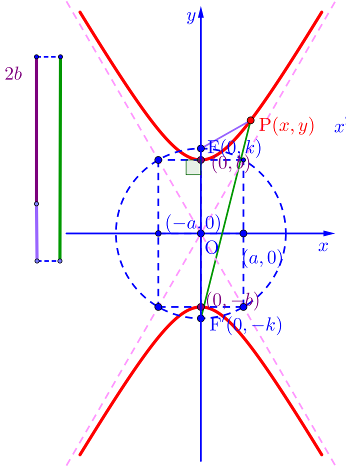

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Github:
https://min7014.github.io/math20200610001.html

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