두 초점이 $(k,0)$, $(-k,0)$ 이고 길이의 차가 $2a$ 로 주어 졌을 때 쌍곡선의 방정식

(The equation for hyperbola when the two focal points are $(k,0)$, $(-k,0)$ and the difference in length is given by $2a$)

The equation for hyperbola when the two focal points are $(k, 0)$, $(-k, 0)$ and the difference in length is given by $2a$

Start End

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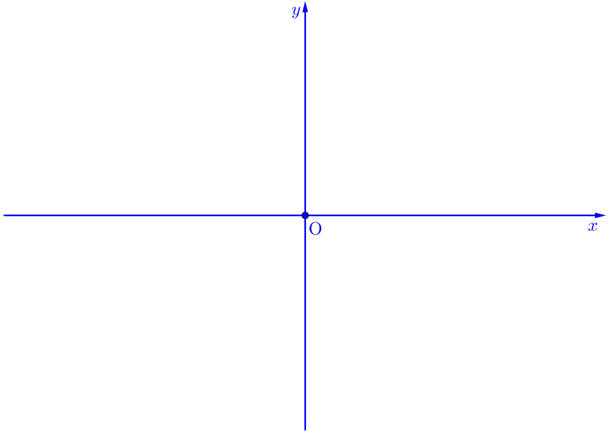

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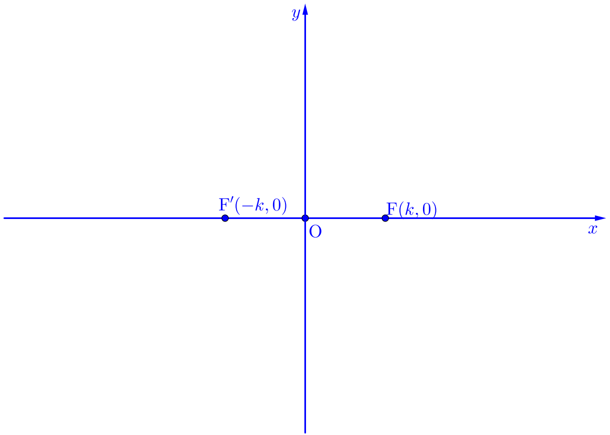

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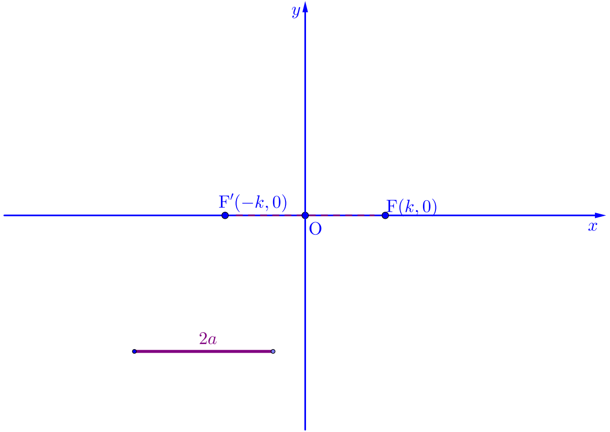

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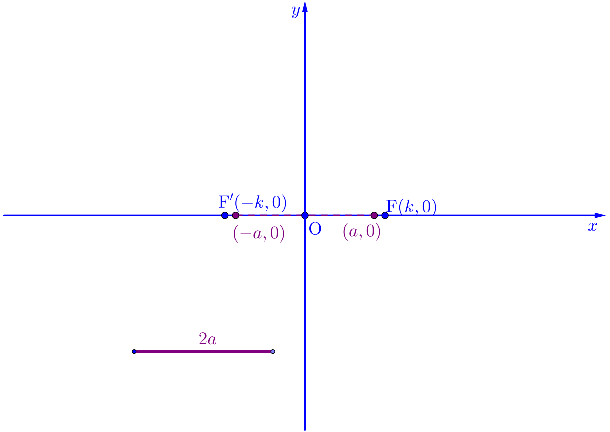

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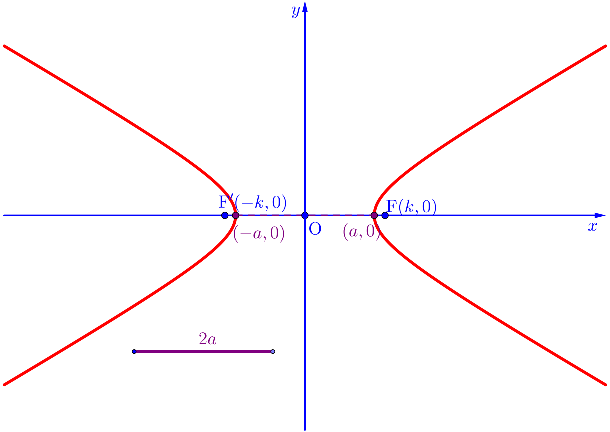

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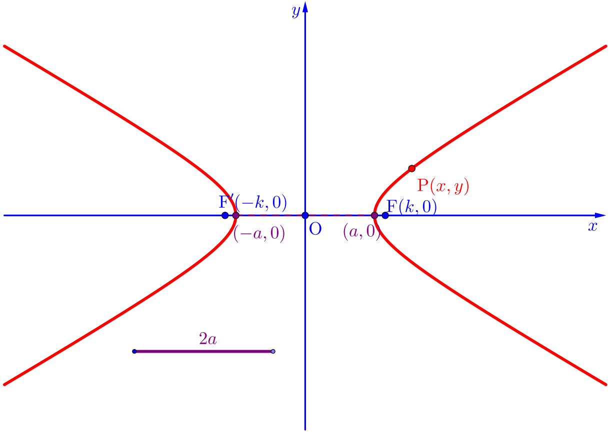

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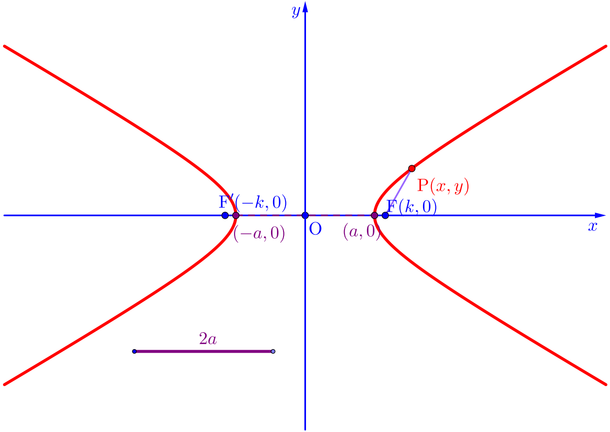

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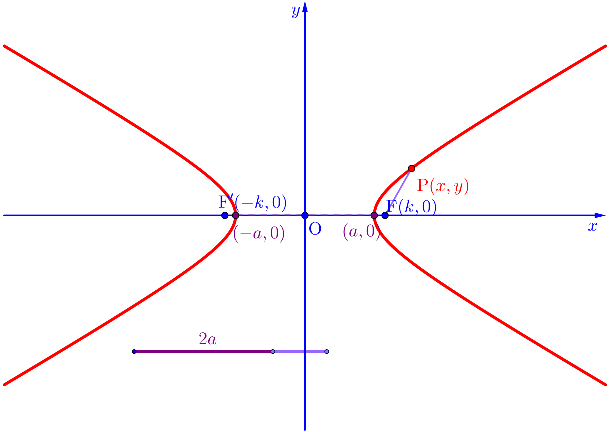

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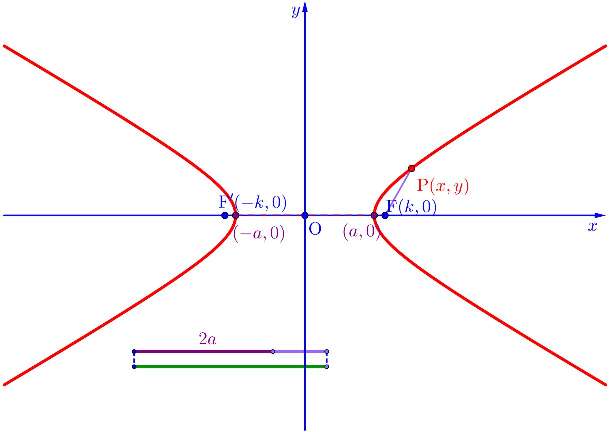

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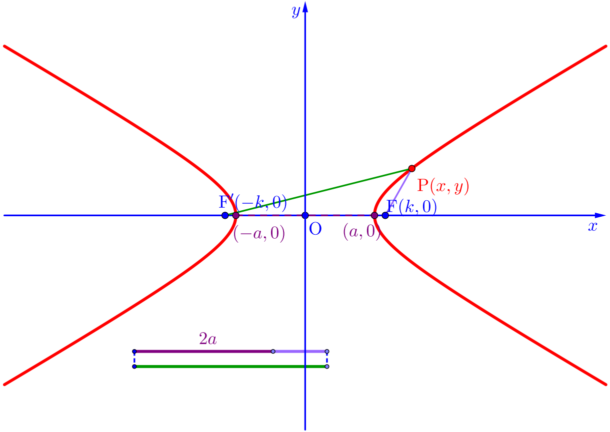

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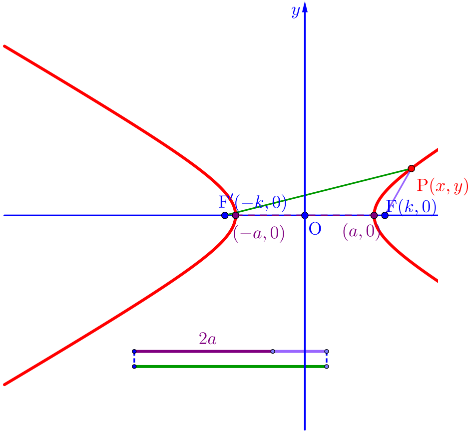

$$\left| \sqrt{(x-k)^2 + y^2} - \sqrt{(x+k)^2 + y^2} \right| = 2a$$

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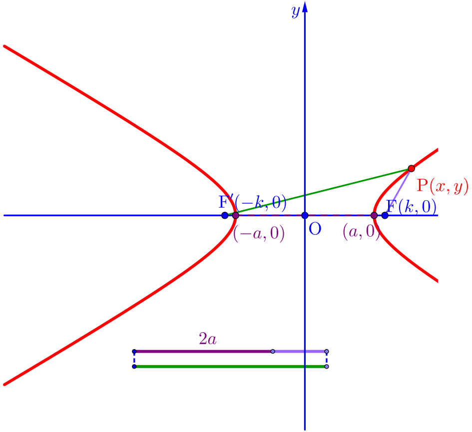

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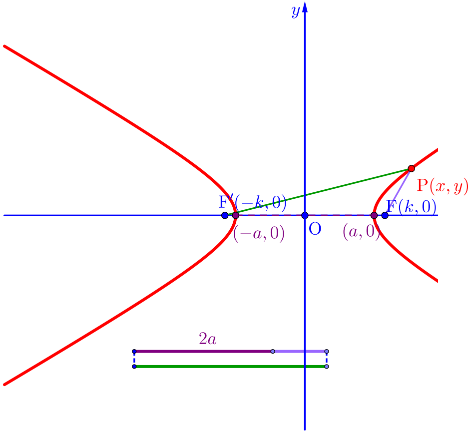

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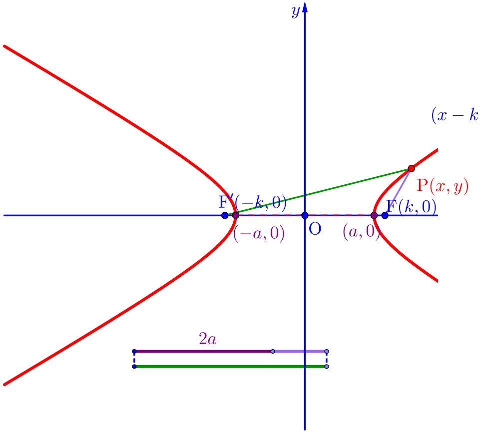

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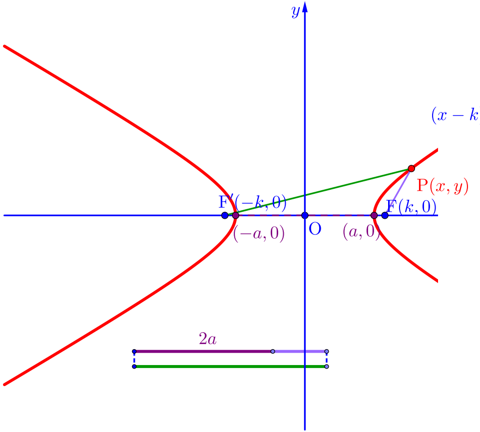

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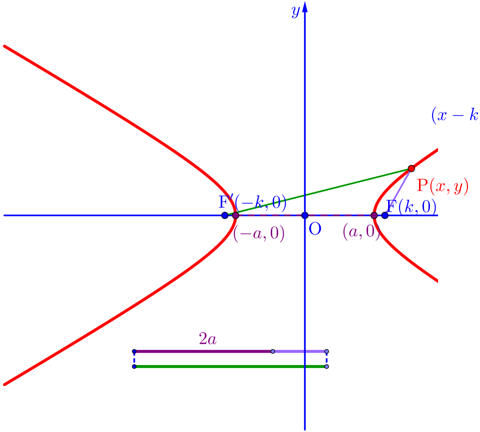

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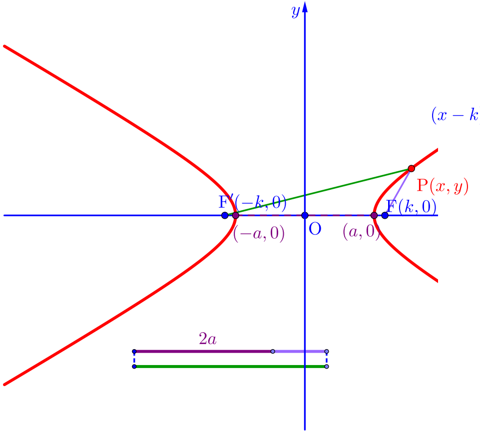

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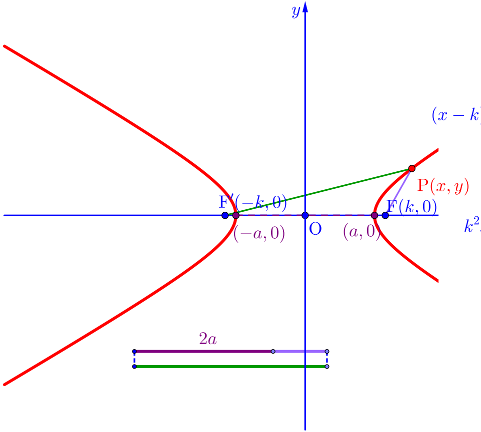

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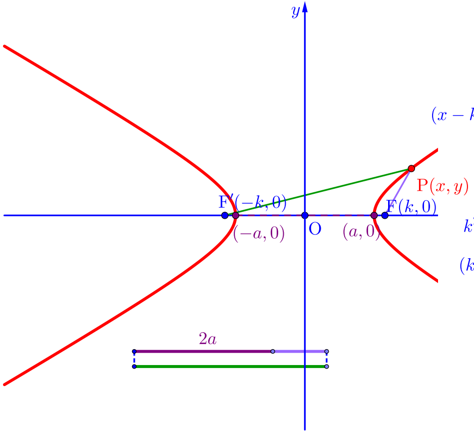

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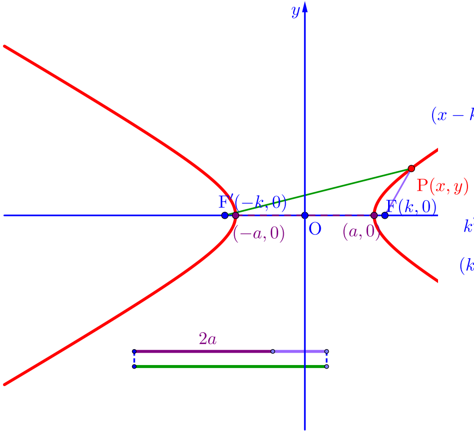

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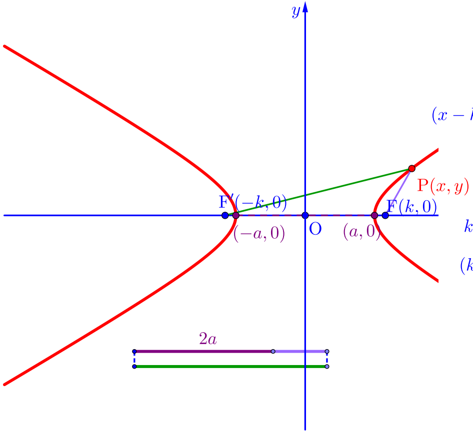

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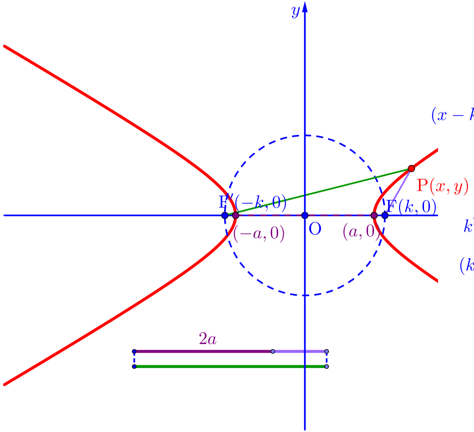

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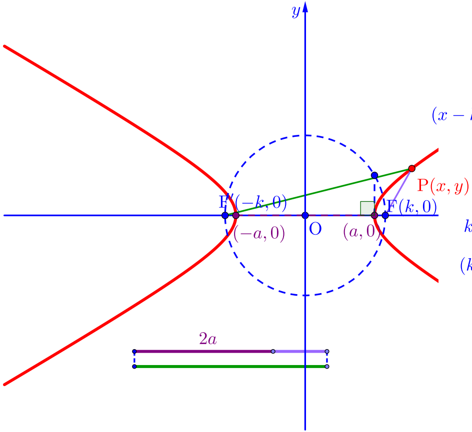

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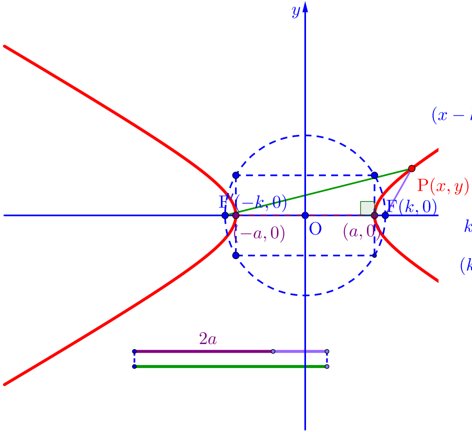

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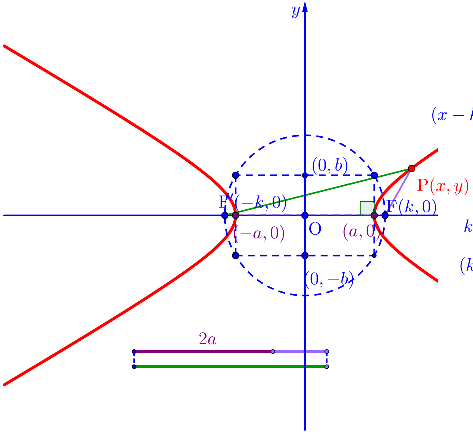

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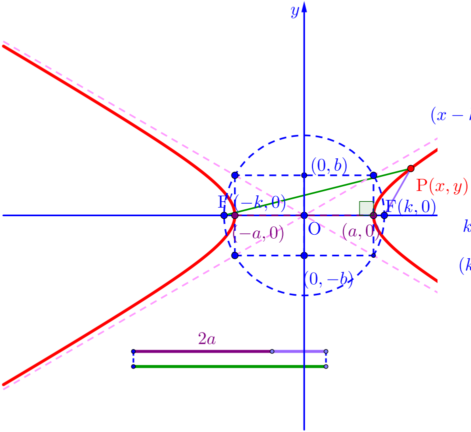

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Github:
https://min7014.github.io/math20200605001.html

Click or paste URL into the URL search bar, and you can see a picture moving.